

Fuzzy Time Intervals for Simulating Actions

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Outline:

- Motivation
 - Why crisp plans and schedules fail?
- PSI project and modeling approach
- Ontology stack and modeling choices
- Minimal model of time – how requirements are met
- Basic (crisp) theory
- Fuzzy extension
 - Time intervals
 - Time phases and periods
- **THROUGHOUT:** How to use for simulating actions

- Conclusions and outlook

Why Crisp Plans and Schedules Fail?

At execution time a design manager ...

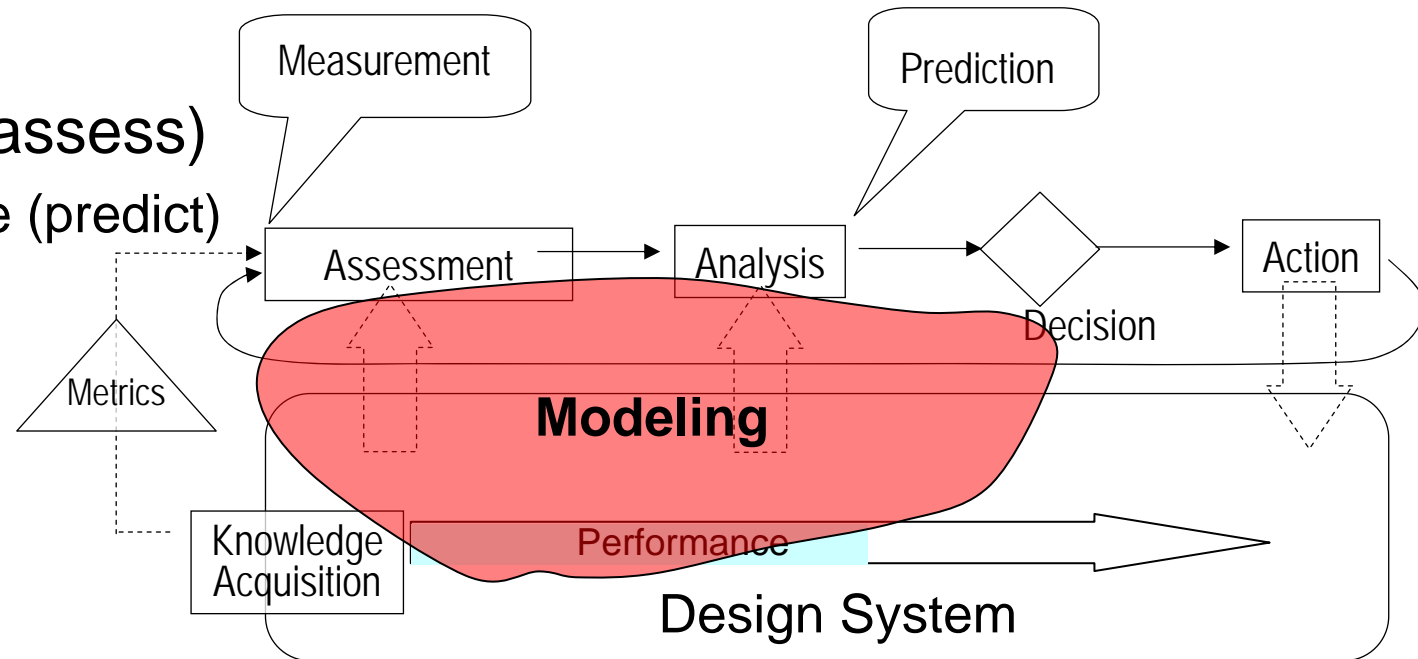
- May find out that:
 - A designer is not available at 08:00:03.1458 CET as planned
 - Designer D will not accomplish activity A at 08:00:03.1458 CET as he swore
- Observes that:
 - Designer D is less busy in other projects than he reports
 - Resource R will be depleted more quickly than estimated
 - Designer D is not that well trained for using tool T as he claims
 - Factually required No of debug-verify iterations will be more than planned
 - Different designers will spend different times for ramping up for activity A
 - Ramping up longer may result in doing the job quicker
 - But, ... not at all necessarily
- Nobody is (crispily) perfect

Performance Simulation Initiative

- R&D project of Cadence Design Systems GmbH
 - Goal: Assess and Manage Performance in Engineering Design
 - Domain: Microelectronics and Integrated Circuits
 - Method: knowledge-intensive simulation of:
 - A Design System and
 - A Dynamic Engineering Design Process
- A “horizontal” framework:
 - Plugged-in focused activities
 - Cooperation with other projects
 - PRODUKTIV+ (BMBF, <http://www.edacentrum.de/produktivplus/>)
 - ACTIVE IP (EC FP7, <http://active-project.eu/>)

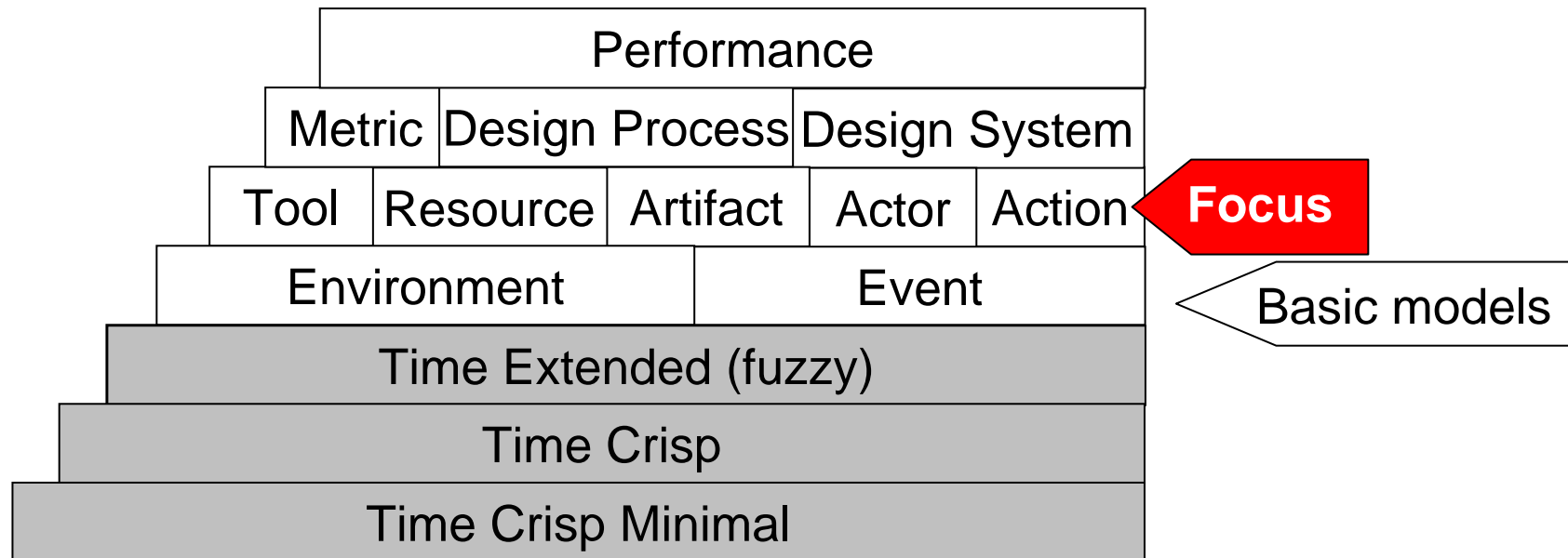
How to Lower Failure Risks in Performance?

- Measure
- Analyze (assess)
 - Simulate (predict)
- Decide
- Apply corrective actions



- For all that: **MODEL ADEQUATELY** to real world and common sense

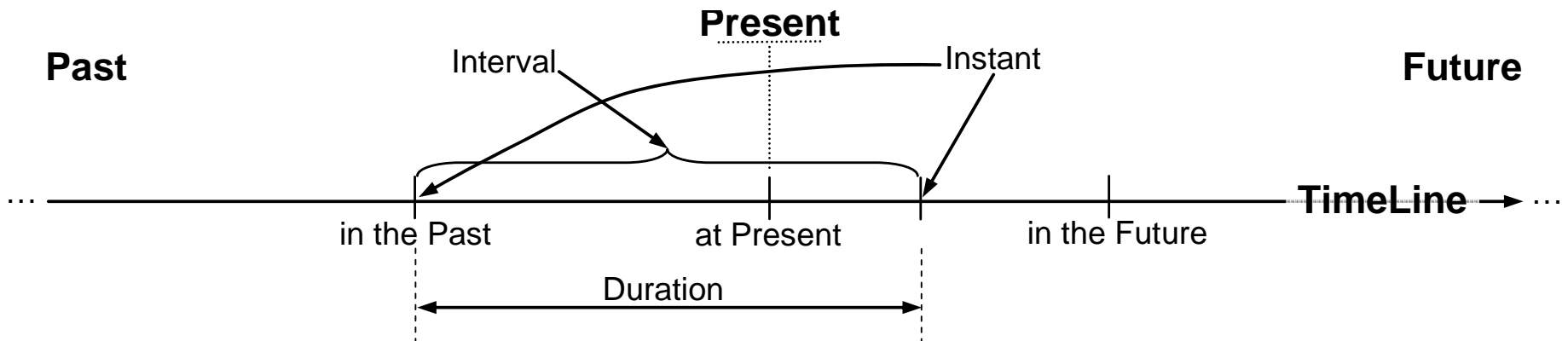
Model (Ontology) Stack



How to **MODEL ADEQUATELY**? - One possible way: Fuzzy Time Intervals

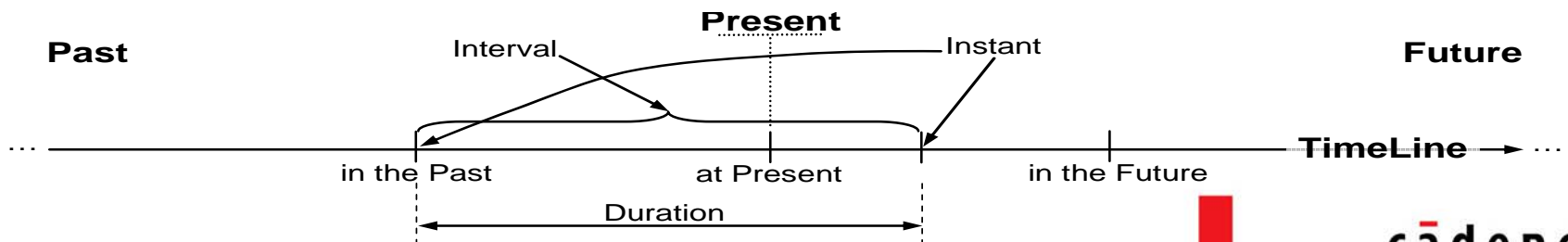
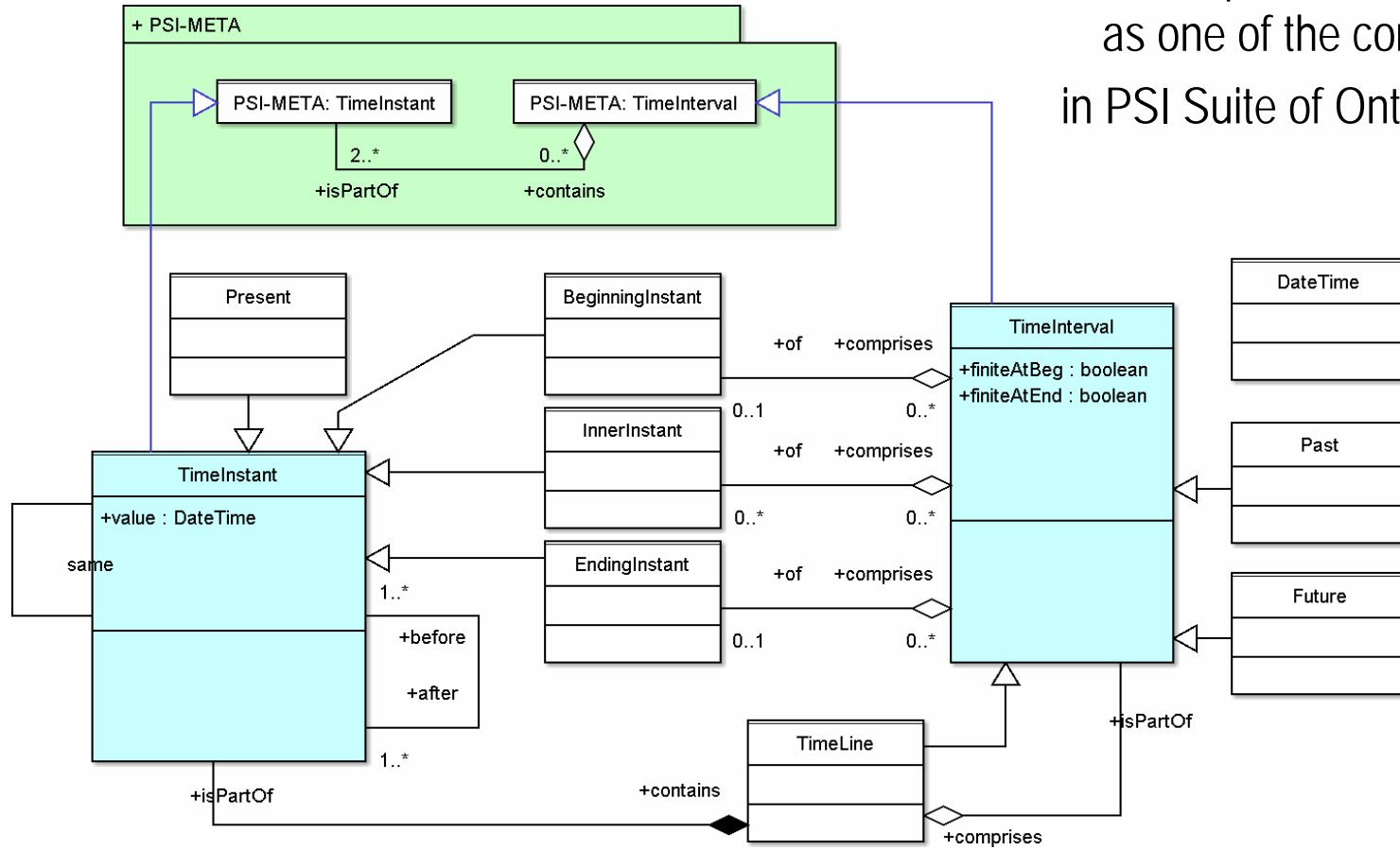
Modeling Choices

- Keep trivial, however efficiently applicable
 - Time is: linear, anisotropic, discrete
- Make effective for modeling actions in processes
 - Properly extend basic (crisp) theory
 - Time intervals are fuzzy
 - Finite and infinite intervals
 - Phases and periods



Time Minimal

Implemented in OWL-DL
as one of the core ontologies
in PSI Suite of Ontologies v.2.2

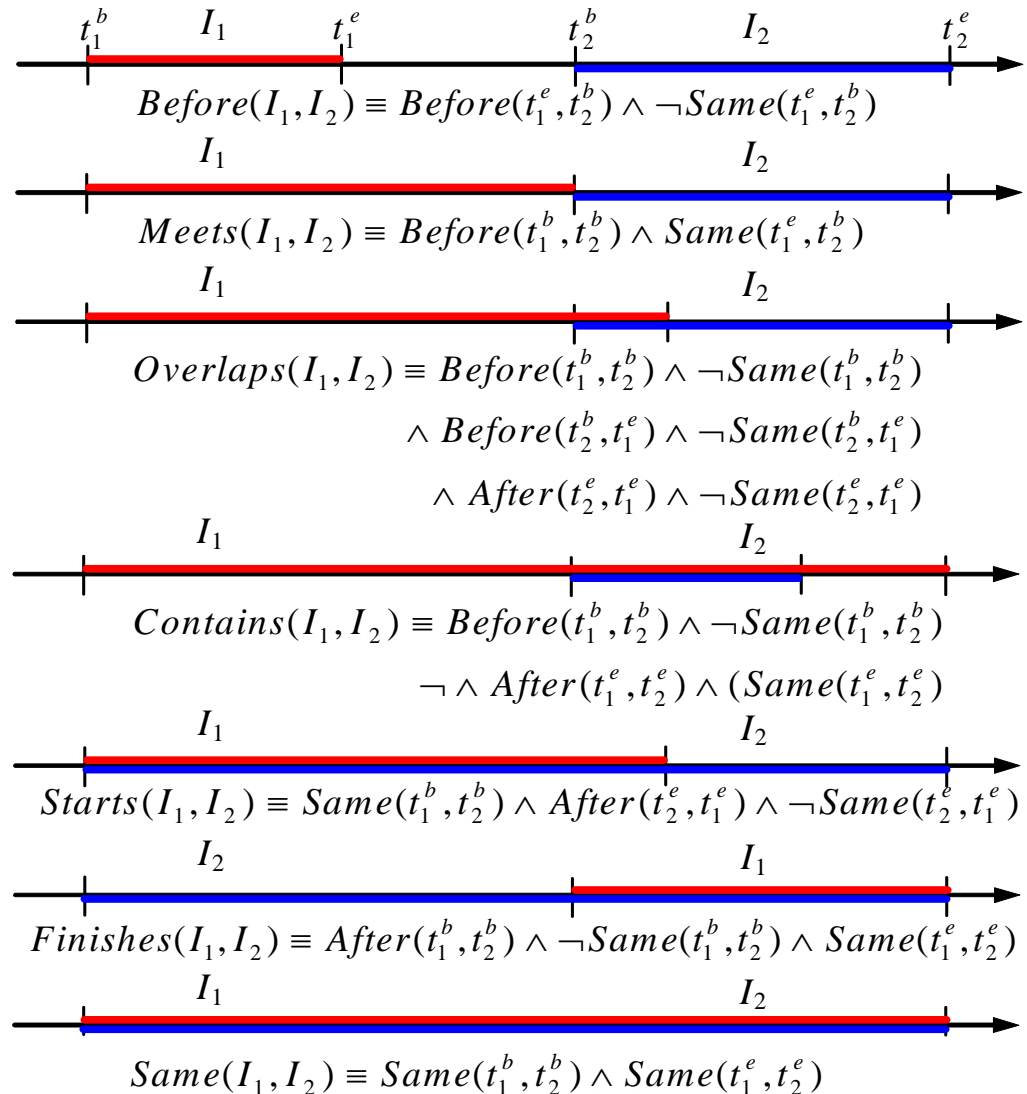


How Requirements are Met?

- Covered:
 - Absolute time points
 - Differently structured and grained time stamps
 - Time intervals and their durations
 - Time intervals open or closed by beginning and ending instants
- Partially covered:
 - Finite and infinite time intervals
- Not covered:
 - Relationships on intervals, vagueness, phases and periods, subjective perceptions, infinity, many more ...

Time Crisp: Allen's Theory

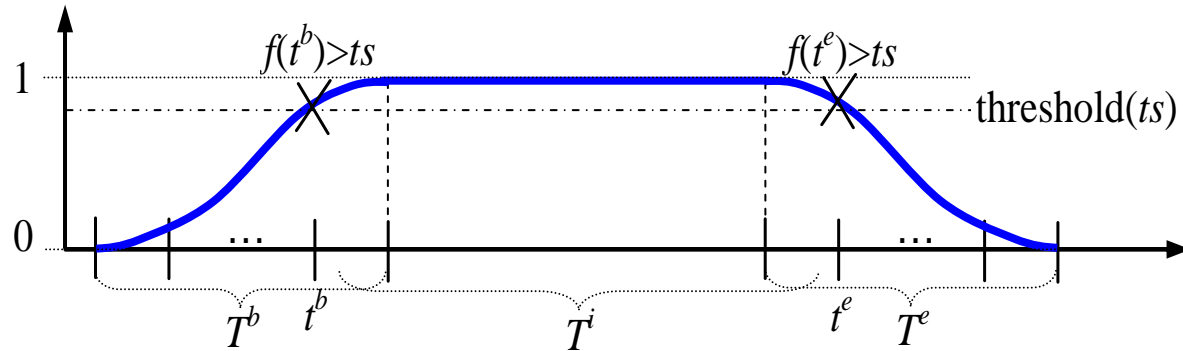
- Extension of Time Minimal
- Interval relationships expressed using relationships among instants
- Implemented in OWL-DL
 - Draft release candidate for PSI Suite v.2.3



Time Fuzzy: Extension of Time Crisp

- Fuzzy time interval:

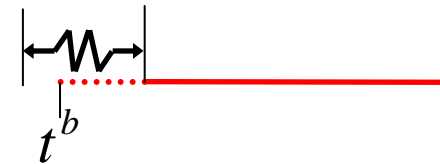
$$I = \{T^b, T^i, T^e, f\}$$



- T^i - the Core – inner instants
- Beginning and Ending sets:

– Beginning ($T^b = \{t_j^b\}$): $\forall t_j^b : t_j^b > t^b \rightarrow t_j^b \in T^i$

– Ending ($T^e = \{t_j^e\}$): $\forall t_j^e : t_j^e < t^e \rightarrow t_j^e \in T^i$

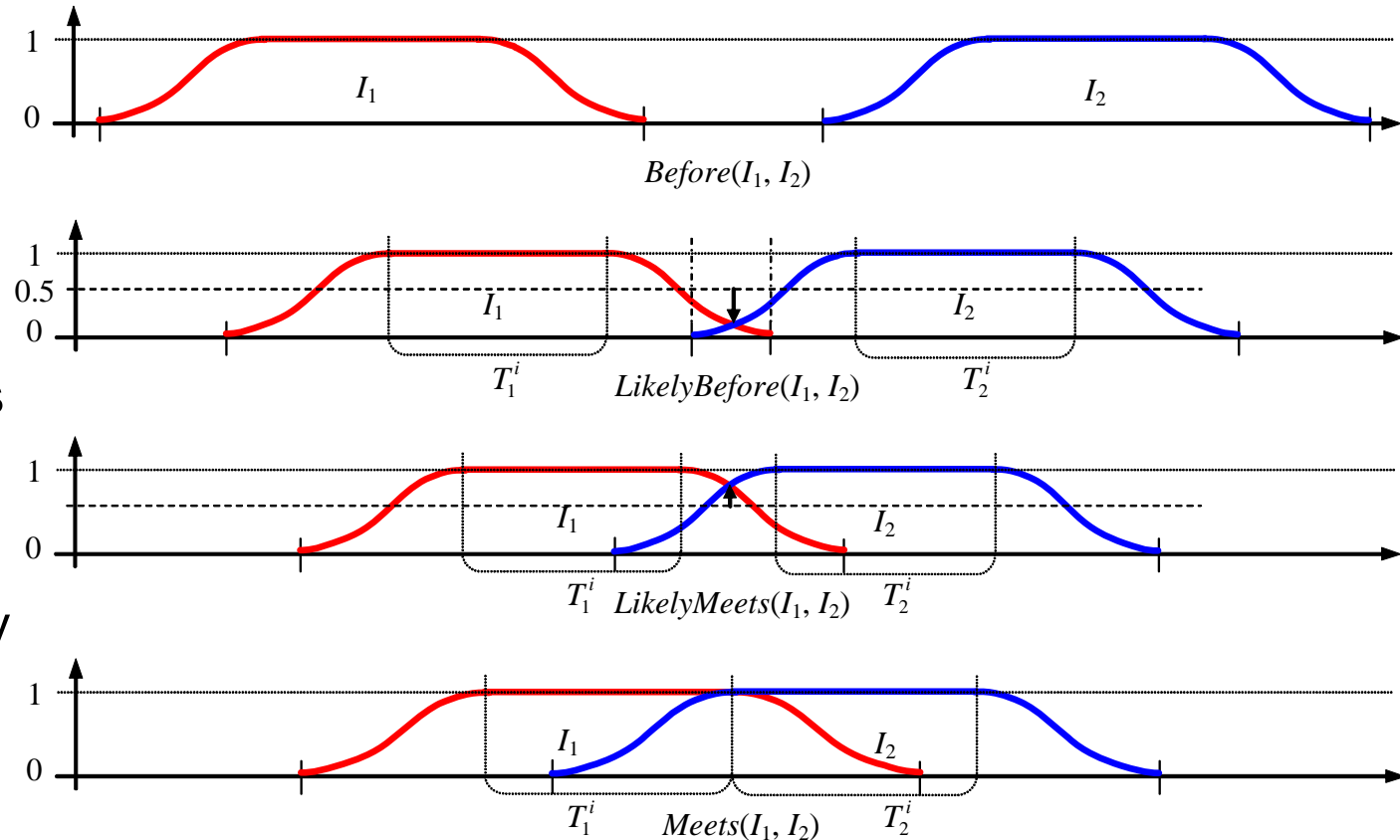


- Discrete membership function: $f : Z \rightarrow [0,1]$ - individual for A-s, R-s, ...
- Thresholds: reputation and confidence
- Implementation issues:
 - Low expressiveness of OWL-DL ...
 - Computational overhead ...

Time Fuzzy: Extension of Time Crisp

Relationships on Intervals 1 of 2

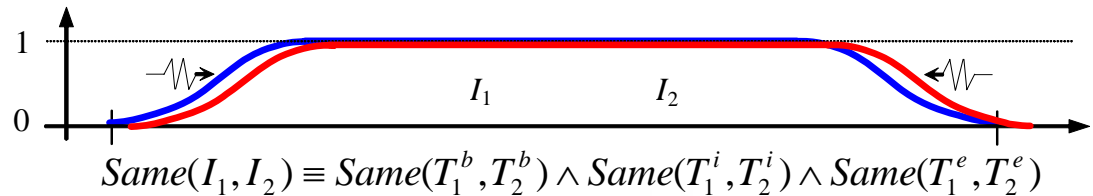
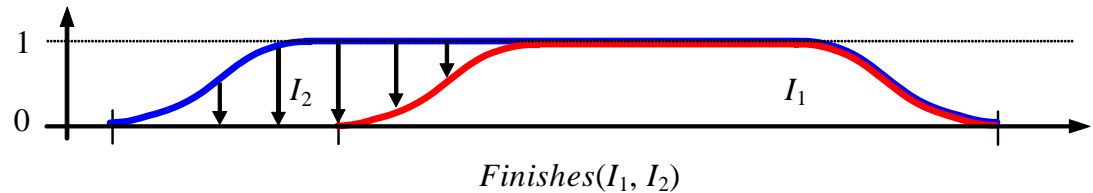
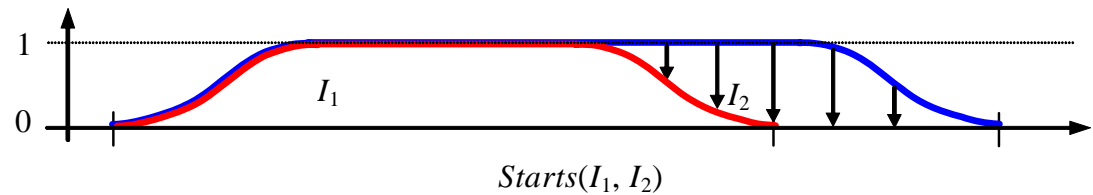
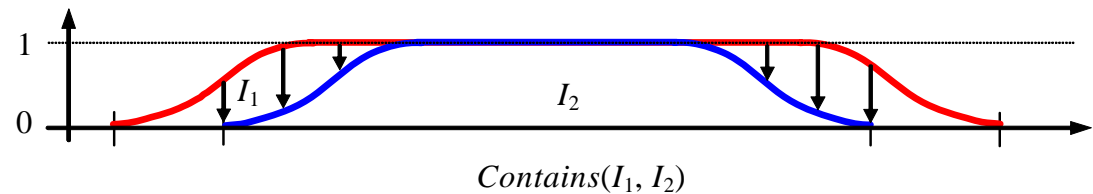
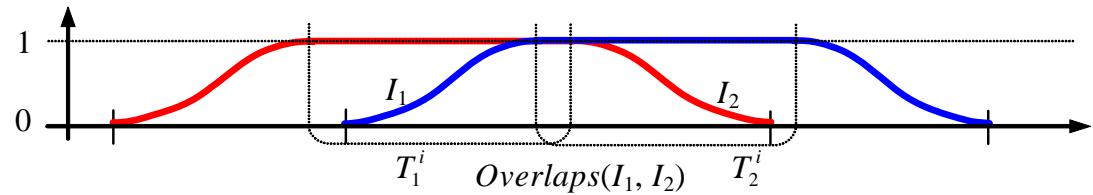
- Approach similar to Crisp
- Correctly degenerates to Crisp
- Substantially more expressive



Time Fuzzy: Extension of Time Crisp

Relationships on Intervals 2 of 2

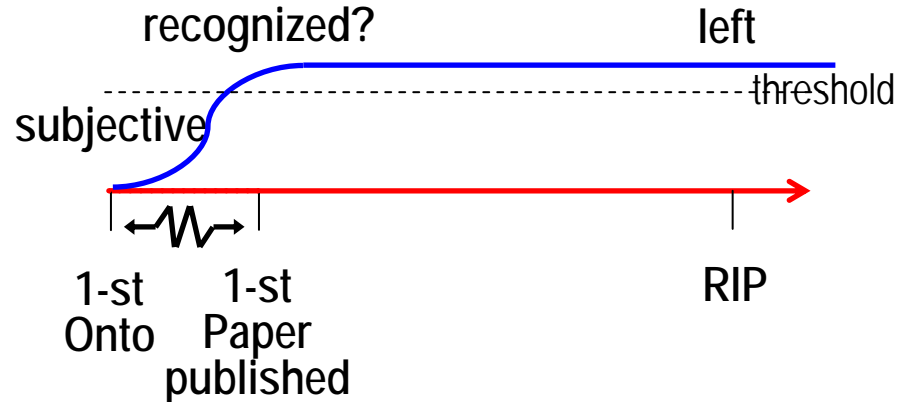
- Expressiveness gain:
 - Relaxation on interval ends
 - More shades in intersection and similarity
- E.g.:
 - $Same(I_1, I_2)$
 - Not always true in Crisp sense
 - Is true when:
 - Either $f_1 \equiv f_2$
 - Or begs and ends contain one instant



Finite and Infinite Intervals

Fuzzy: modeling vague durations of events and actions

- From now on I'm a knowledge engineer!
 - My first naïve ontology is accomplished
- Crafting ontologies? – never more:
 - My first paper was badly rejected
- At least:
 - the Sun always shines ...



$I^\infty :$

$$T^e = \emptyset, \forall t_j \in T^i \exists t_i : (t_i \in T^i) \wedge \text{After}(t_i, t_j)$$

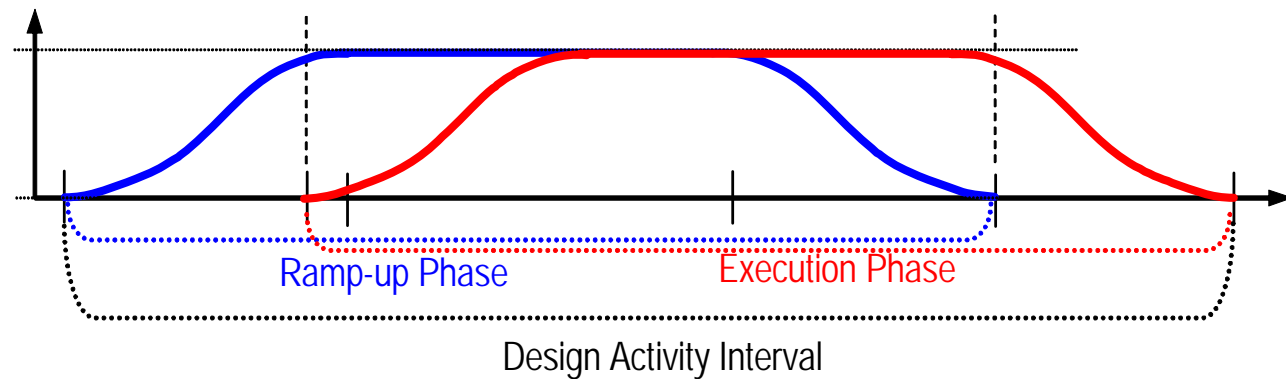
${}^\infty I :$

$$T^b = \emptyset, \forall t_j \in T^i \exists t_i : (t_i \in T^i) \wedge \text{Before}(t_i, t_j)$$

${}^\infty I^\infty :$

$$T^b = \emptyset, T^e = \emptyset, \forall t_j \in T^i \exists t_i, t_k : (t_i, t_k \in T^i) \wedge \text{Before}(t_i, t_j) \wedge \text{After}(t_k, t_j)$$

Phases



- Phases of an Activity: sub-activities
 - Often have facilitation dependencies:
 - The more effective the source – the more efficient the target
 - E.g.: Ramp-up and Execution phases of a design Activity
- Durations of phases:
 - Subjective
 - Vague
- Modeled using Fuzzy interval sets $S = \{s_1, \dots, s_i, s_{i+1}, \dots, s_N\}$

$$\forall i = 1..N - 1, j = i + 1, (LikelyMeets(s_i, s_j) \vee Meets(s_i, s_j))$$

$$Same(\bigcup_{i=1}^N s_i, I)$$

Periods

- Associated with regular or repeating events
 - Sunrise, breakfast, blames by the project manager
- Finite or infinite sets of periods
- Finite: $\Pi = \{\pi_1 \dots \pi_i, \pi_{i+1}, \dots, \pi_N\}$
 - Order: $\forall i = 1..N-1, j = i+1..N (Before(\pi_i, \pi_j) \vee Meets(\pi_i, \pi_j))$
- Infinite:
 - ${}^\infty \Pi = \{\dots \pi_i, \pi_{i+1}, \dots, \pi_n\}$ - at the beginning
 - $\Pi^\infty = \{\pi_1 \dots \pi_i, \pi_{i+1}, \dots\}$ - at the end
 - ${}^\infty \Pi^\infty = \{\dots \pi_i, \pi_{i+1}, \dots\}$ - at both ends
 - Order: ${}^\infty \Pi^\infty : \forall i \exists j : (Before(\pi_i, \pi_j) \vee Meets(\pi_i, \pi_j))$
 - $\Pi^\infty : \forall i \exists j > 1 : (Before(\pi_i, \pi_j) \vee Meets(\pi_i, \pi_j))$
 - ${}^\infty \Pi : \forall i < n \exists j : (Before(\pi_i, \pi_j) \vee Meets(\pi_i, \pi_j))$

Conclusions and Outlook

- Did not plan to refine fuzzy reasoning ...
 - Similar to (at least) two other approaches, but in different domains
- One of the basic models for reasoning about events and actions – in PSI
 - Used in Dynamic Engineering Design Process scheduling and simulation
 - Provides more flexible process representations
 - By “springing” events and actions using fuzzy time intervals Allows representing subjective perceptions
 - More realistic phases and periods
- Time Minimal, Crisp, Fuzzy:
 - Minimal – implemented, used in PSI software
 - Crisp – implemented as a draft release candidate
 - Fuzzy – in implementation
 - Some minor technical problems in representation and efficiency

Questions Please

